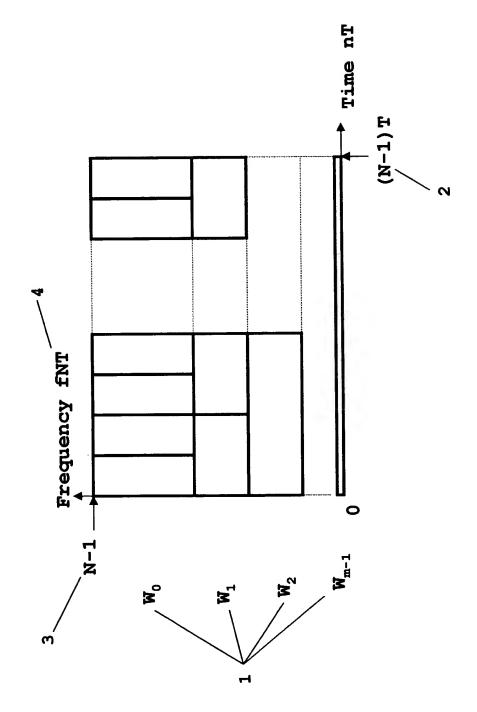
FIG. 1 Wavelet Tiling of an N-Point Digital t-f Space



Wavelet Iterated Filter Bank for Tiling t-f Space in FIG. ~ FIG.

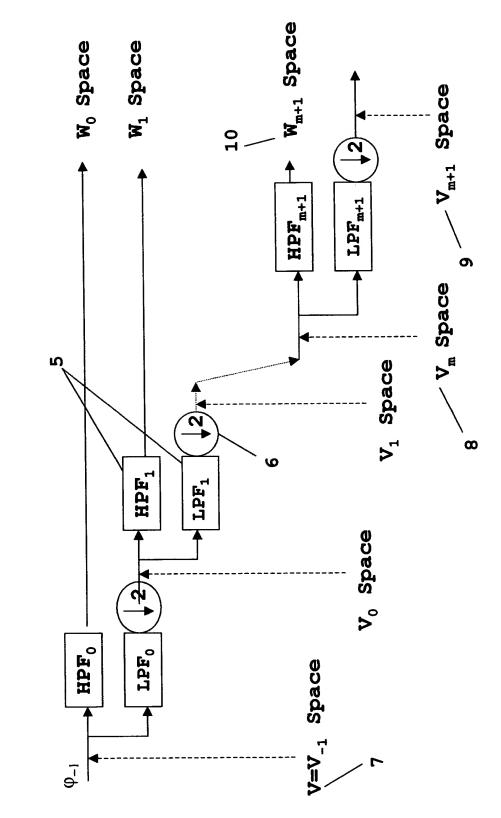
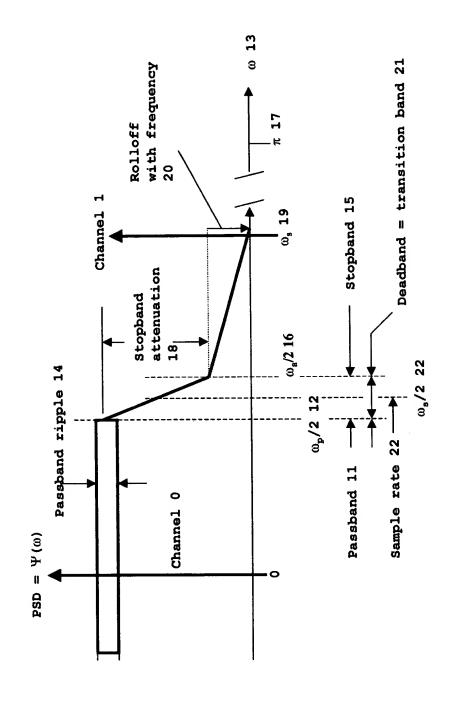


FIG. 3 PSD Requirements for Communications



LS Metrics and Cost Function FIG.

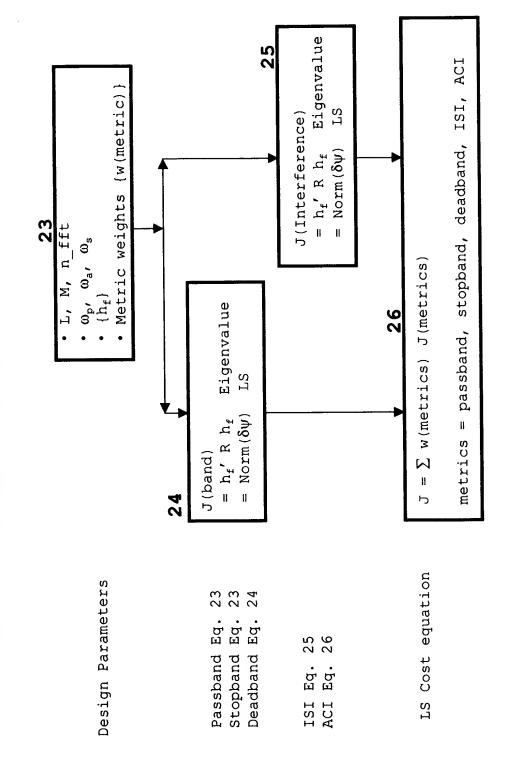


FIG. 5A LS RECURSIVE DESIGN ALGORITHM IN MATLAB 5.0 CODE TO DESIGN:

- MOTHER WAVELET IN FIG. 6
- NEW WAVELET FROM MOTHER WAVELET

```
Σ
                                                                                                                                                                                                                                                                         0
                                                                                                                         nominal Wavelet length in units of
                                                                                                                                                                                                                                                                                                                    maximum number of channels allowed
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    % number of iterations for LS design
                                                                                                                                                                                                                                                                                                                                                   % wp/2pi edge of passband
% ws/2pi edge of stopband
                                                                                                                                                                                                                       FFT size for spectrum centered at
                                                                                                                                                                       = normalized Wavelet sample rate
                                                                                                                                                                                                                                                      dB, channel-to-channel imbalance
                                                                                                                                                                                          normalized channel passband
                                                                                                                                                                                                                                                                                                                                                                                    edge of passband
                                                                                                                                                         normalized channel spacing
                                                                                                                                                                                                          number of design harmonics
                                                                                                                                                                                                                                                                                                                                                                                                   % edge of stopband
                                                                                                                                                                                                                                                                                                                                      % 0.5 * Wavelet sample rate
- PERFORMANCE DATA AND PLOTS
                                                                                                           % Wavelet sample interval
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    weighting for deadband
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     % weighting for passband
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    stopband
                                                                                                                                          Wavelet length N =ML+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    weighting for ISI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    weighting for ACI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     weighting for
                                                                                                                                                                                                                                                                                                      % definition
                                                                                                                                                                                                                                        dB, Eb/No
                                                                                                                                                                                                                                                                                                                                                                                                                                     % STEP 1.3 OPTIMIZATION PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                    floor(f_pass*n_fft)
floor(f_stop*n_fft)
                                            & STEP 1 DESIGN PARAMETERS
                                                                             % STEP 1.1 SCENARIO PARAMETERS
                                                                                                                                                                                                                                                                                        & STEP 1.2 DERIVED PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                       = (2-fp)/(M*fs)
                                                                                                                                                                                                                                                                                                                                      = (n_fft/M)
                                                                                                                                                                                                                                                                                                                                                     = fp/(M*fs)
                                                                                                                                                                                            0.8864;
                                                                                                                                                                                                                                                                                                        = pi*2;
                                                                                                                                                                                                                         = 1024;
                                                                                                                                                                                                                                        = 6.0 ;
= 6.0 ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       2.e-3
                                                                                                                                             = M*L+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      = 1.e-2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     = 0.80
                                                                                                                                                                                                          = 16
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       n iteration = 10;
                                                                                                                            = 16;
                                                                                                                                                                                                                                                                                                                                                                                                                           11
                                                                                                                                                                                                                                                         x_imbal_aci
                                                                                                                                                                                                                                                                                                                                                                                   nfft_pass
                                                                                                                                                                                                                                                                                                                                                                                                      nfft_stop
                                                                                                                                                                                                                                                                                                                                        nfft wsr
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       alpha_4
alpha_5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       alpha 1
alpha 2
alpha 3
                                                                                                                                                                                                                                                                                                                                                        f_pass
f_stop
                                                                                                                                                                                            fp
n_f
n_fft
                                                                                                                                                                                                                                                                                                          twopi
                                                                                                                                                                                                                                            epno
                                                                                                                                                            Ęs
```

FIG. 5B

```
STEP 2.4 MATRIX "c matrix" USED FOR ISI,ACI LS ERROR METRICS J(ISI)IN EQ. 25 AND J(ACI) IN EQ. 26
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  EQ. 23 AND FUNCTION "pmn_d" CACULATES ERROR MATRIX FOR J(DEAD) IN EQ. 24
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      STEP 2.3 FUNCTION "pmn" CALCULATES PASSBAND, STOPBAND LS ERROR MATRICES FOR THE METRICS J(PASS), J(STOP) IN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          8 STEP 2.5 PASSBAND, STOPBAND, WAVELET SAMPLE RATE TEMPLATES
                                                                                                                                                                                                                                                                                                                                                                             8 STEP 2.2 MATRIX "bw matrix" MAPS WAVELET FREQUENCY DESIGN
8 HARMONICS INTO WAVELET TIME RESPONSE
                                                                                                                                                                                                                                                                                                                                                                                                                                                             bw_matrix = zeros(m,n_f);
for 1_r=1:m
    ang = 2*p1* rem( (i_r)*(0:n_f-1)/(N-1),1); % time
bw_matrix(i_r + 1, :) = 2 * cos(ang);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            v 1 = 1:nfft_pass+1;
v_2 = nfft_pass+2:nfft_stop;
v_3 = nfft_stop+1:nfft_stop+nfft_pass;
hw_ref= [zeros(size(v_1)) -110*ones(size(v_2)) ...
zeros(size(v_3))];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     %===set up wavelet sample rate templet
v_lb = l:nfft_wsr;
v_2b = nfft_wsr+1:nfft_wsr+1;
v_3b = nfft_wsr+2:nfft_wsr+nfft_pass+nfft_stop;
hw_wsr= [-110*ones(size(v_lb)) zeros(size(v_2b))
& STEP 2 INITIALIZATION CALCULATIONS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    s===set up passband and stopband templet
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               c matrix=[bb; flipud(bb(1:m,1:(m+1)))]/2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           au=eye(m+1,m+1); % identity matrix
                                                            STEP 2.1 WAVELET LENGTH PARAMETERS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        matrix(m+1,1)=c_matrix(m+1,1)*2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       % rotation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                bw_{matrix(1,:)} = ones(1,n_f);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    -110*ones(size(v 3b))];
                                                                                                                                                                                                                                                                               N is even
                                                                                                              nodd= fix( N/2 );
nodd = N - 2 * nodd ;
if ( nodd == 1)
m = (N - 1 ) /2 %
                                                                                                                                                                                                                                                                               ф
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bb=rot90(au);
                                                                                                                                                                                                                                                                               m = N/2;
                                                                                                                                                                                                                              nrow = m+1;
                                                                                                                                                                                                                                                                                                           nrow = m;
                                                                                                                                                                                                                                                                                                                                     end
```

FIG. 5C

```
% STEP 3 PASSBAND, STOPBAND, DEADBAND LS ERROR MATRICES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          STEP 3.4 WEIGHTED LS ERROR MATRIX "P_total" FOR THE WEIGHTED SUM OF J(PASSBAND), J(STOPBAND), J(DEADBAND)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 p_total= alpha_1*passband+alpha_2*stopband+alpha_5*deadband;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     STEP 3.5 CONVERT IS ERROR MATRIX IN TIME "p_total" TO LS ERROR MATRIX IN FREQUENCY "pw_t"
                                                                                                                                                                                                                                                                    & STEP 3.2 J(STOPBAND) LS ERROR MATRIX "stopband"
                                                                  % STEP 3.1 J(PASSBAND) LS ERROR MATRIX "passband"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           % STEP 3.3 J(DEADBAND) LS ERROR MATRIX "deadband"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           %deadband = pmn_d( omega_l, omega_u, N, an) ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             pw_total = bw_matrix'*(p_total*bw_matrix);
                                                                                                                                                                                                                passband = pmn( omega_1, omega_u, N, an);
                                                                                                                                                                                                                                                                                                                                                                                                                       stopband = pmn( omega_l, omega_u, N, an) ;
                                                                                                                                           omega_u = f_pass * pi ; % 0.0554
an=ones(1,nrow);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          deadband = zeros(nrow,nrow);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         omega_l = f_pass * pi;
omega_u = f_stop * pi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                             omega_l = f_stop * pi;
omega_u = pi;
                                                                                                                               omega_1 = 0.0 * pi;
                                                                                                                                                                                                                                                                                                                                                                                               an=zeros(1, nrow);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 pw_t = pw_total;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    an=ones (1, nrow);
```

2

SIEP 4 ITERATIVE EIGENVALUE SOLUTION

FIG. 5D

```
% STEP 4.1 FOR EACH ITERATION "i_iteration" FIND EIGENVECTOR
% IN FREQUENCY THAT MINIMIZES THE COST FUNCTION J IN
EQ. 27 WHOSE LS ERROR MATRIOX IS "pw_t"
xstop = max(hw_db(nfft_stop+1:nfft_stop+nfft_pass+1) );
                                                                                                                                                                                                                                                               - WAVELET FREQUENCY DESIGN HARMONICS "hw_eig"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               scale ww = 1. / (hmax^2); \$ normalized hn is the normalized Wavelet response
                                                                                                                                                                                                                                                                                       - WAVELET IMPULSE RESPONE IN TIME "hn"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    %Fourier transform of hn & hn in the next channel
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      arg_rot = twopi* rem( (0:N-1)*ich /nc , 1 );
[freq, hw db] = freq_rsp(hn, arg_rot, n_fft);
% hn_data = [hn_data hn'];
% hw_data = [hw_data hw_db'];
                                                                                                                                                                                                                                                                                                                                                  b_vector = bw_matrix * eig_vec(:,min_index);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           %===== peak_to_peak ripple in passband
max_ripple = max( hw_db(1: nfft_pass+1));
min_ripple = min( hw_db(1: nfft_pass+1));
xripple = max_ripple - min_ripple ;
%=== stopband_atttenuation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  % STEP 4.3 PASSBAND RIPPLE "xripple" AND
% STOPBAND ATTENUATION "xstop"
                                                                                                                                eig_val = eig(pw_t);
[eig_vec eigval] = eig(pw_t);
[eigval_min,min_index] = min(eig_val);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         hn(1:m) = 0.5*b vector((m+1):-1:2);
hn(m+1) = b vector(1);
hn(m+2:N) = hn(m:-1:1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      hn(m:-1:1) = 0.5 * b_vector(1:m);
                                                                                                                                                                                                                                                                                                                                                                        hw_eig = eig_vec(:,min_index);
hw_eig(1) = 2*hw_eig(1);
hw_max = max(hw_eig);
hw_eig = hw_eig/hw_max;
if ( nodd == 1) % N is odd
                                                                                                                                                                                                                                         & STEP 4.2 MAP EIGENVECTOR INTO:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              hn(m+1:1:2*m) = hn(m:-1:1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           hmax = max(abs(hn));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            nn = hn/ hmax;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               end & nodd
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ich = 0;
                                                                                                                                                                                                                                                                                                                            ====
```

FIG. SE

33

```
- METRICS J(ISI) = "errM_isi" AND J(ACI) = "errM_aci"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            - SNR ERROR CONTRIBUTORS "errv isi" AND "errv aci"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          % ISI error residual vector w_vector
w_vector(k_wave+1)=w_vector(k_wave+1)+hn(ii+1)*hn(ii+1+...
nc*k_wave);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             scale_isi_aci = 1/w_vector(1);
w_vector = w_vector * scale_isi_aci;
errV isi = sum(w_vector(2:M) .*w_vector(2:M)); %ISI LS error
%2-sided power summation of isi residual errors
errV_isi = 2. * errV_isi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               - MATRICES "w_matrix" AND "w_f_matrix"
8 STEP 5 WEIGHTED LS ERROR METRICS FOR:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            a_matrix(i_r+1, nic) = hn(nic - n_cc);
                                                                                                                                               err_pass = b_vector' * passband * b_vector;
err_stop = b_vector' * stopband * b_vector;
err_dead = b_vector' * deadband * b_vector;
beta_pass = alpha_1 * err_pass;
beta_stop = alpha_2 * err_stop;
beta_dead = alpha_5 * err_dead;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               - LS ERROR MATRIX "w_matrix"

- J(ISI) = "errM_isi"

- SNR LOSS ISI ERROR "errV_isi"
                                 - J(PASSBAND) = "beta_pass"
                                                           - J(STOPBAND) = "beta_stop"
- J(DEADBAND) = "beta_dead"
                                                                                                                                    for ir = 0:m

n cc = ir * nc;

if ( i r>=1 & ir<=M)

nic = (n cc+1):(2*m+1);
                                                                                                                                                                                                                                                                                                                                                                                                        & STEP 6 ISI AND ACI LS:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 a_matrix= zeros(m+1,2*m+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               n_i = N - 1 - k_wave*nc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            w vector(k wave+1) = 0.;
                                                                                                - J (DEADBAND)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              STEP 6.1 J(ISI):
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for k wave = 0:M
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for ii = 0:n i
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     40000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          end
                                                                                                                                                                                                                                                                                                                                                                         34
```

8====

FIG. 5E

33

```
- MATRICES "w matrix" AND "w f matrix"
- METRICS J(ISI) = "errM isi" AND J(ACI) = "errM aci"
- SNR ERROR CONTRIBUTORS "errV isi" AND "errV aci"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                scale isi aci = 1/w_vector(1);
w_vector = w_vector * scale_isi_aci;
w_vector = w_vector * scale_isi_aci;
errV_isi = sum(w_vector(2:M) .*w_vector(2:M)); %ISI LS error
%2-sided power summation of isi residual errors
errV_isi = 2 * errV_isi;
errV_isi = 2 * errV_isi;
errV_isiMax = max(abs(w_vector(2:M)));
%====a_matrix = m+1 x 2m+1 = A
a_matrix= zeros(m+1,2*m+1);
for i_r = 0:m
n_cc = i_r * nc;
i_r * nc
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for ii = 0:n_i
% ISI error residual vector w_vector
w_vector(k_wave+1)=w_vector(k_wave+1)+hn(ii+1)*hn(ii+1+ ...
& STEP 5 WEIGHTED LS ERROR METRICS FOR:
                                                                                                                                                                                                                                                                                                                err_stop = b_vector' * passband * b_vector;
err_stop = b_vector' * stopband * b_vector;
err_dead = b_vector' * deadband * b_vector;
beta_pass = alpha_1 * err_pass;
beta_stop = alpha_2 * err_stop;
beta_dead = alpha_5 * err_dead;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        - IS ERROR MATRIX "w matrix"

- J(ISI) = "errM isi"

- SNR LOSS ISI ERROR "errV_isi"
                                                                        - J(PASSBAND) = "beta_pass"
- J(STOPBAND) = "beta_stop"
- J(DEADBAND) = "beta_dead"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     nc*k_wave);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   & STEP 6 ISI AND ACI LS:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    n_1 = N - 1 - k_wave*nc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      w_vector(k_wave+1) = 0.;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      STEP 6.1 J(ISI):
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for k_wave = 0:M
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      34
```

FIG. 5G

```
9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     男 男
                                                                                      STEP 7.1 WEIGHTED LS ERROR METRICS FOR ISI, ACI, TOTAL

- WEIGHTED ISI LS ERROR METRIC "beta_isi"

- WEIGHTED ACI LS ERROR METRIC "beta_aci"

- TOTAL LS ERROR METRIC J = "exrm_LS"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                STEP 7.3 UPDATE J LS ERROR MATRIX "PW_t" FOR NEXT ITERATION
                                                                                                                                                                                                                                                                & STEP 7.2 SAVE WEIGHTED LS ERROR METRICS FOR EACH ITERATION
                      UPDATE LS ERROR MATRIX "pw_t" FOR NEXT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       STEP 8.1 SNR LOSSES DUE TO PASSBAND RIPPLE, ISI, ACI, AND THE TOTAL SNR LOSS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     - PASSBAND RIPPLE LOSS "xloss ripple", - ISI LOSS "xloss isi",
                                                                                                                                                                                                                                 errM LS = beta pass+beta stop+beta dead+beta isi+beta aci;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        p_t = p_total+ alpha_3 * w_matrix+ alpha_4 * w_f_matrix
pw_t = bw_matrix'*p_t* bw_matrix;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    "xloss_aci".
"xloss_total",
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   k_delta = 10.^( xripple/2. /20.) - 1.;
kloss_ripple = -10. * log10( 1.0 - x_delta^2 );
#===== isi loss
- WEIGHTED LS ERROR METRICS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          xx_isi = xebno ' 10.0 );
xloss_isi = 10. * log10( 1.0 + xx_isi );
%=====
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     & STEP 8 SIGNAL-TO-NOISE SNR LOSS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   passband ripple loss
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   xebno = 10.^( ebno / 10.0 );
... 'e' = xebno * errV isi ;
                                                                                                                                                                                         beta_isi = alpha_3*errM_isi;
                                                                                                                                                                                                            beta_aci = alpha_4*errM_aci;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     - ACI LOSS
- TOTAL LOSS
                                              ITERATION
                                                                                                                                                                                                                                                                                                                             scale_err = errM_LS;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          isi loss
                                                                                                                                                                                                                                                                                                             if i_iteration==1
7
 & STEP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    8=====
```

IG. 5H

```
STEP 9.1 WAVELET FREQUENCY DESIGN HARMONICS "hn_eig
                                                                                                                                                loss_LS =[loss_LS ; i_iteration xloss_total ....
xloss_ripple xloss_isi xloss_aci ];
                                                                           STEP 8.2 SAVE SNR LOSSES FOR EACH ITERATION
                                                                                                                                                                               & STEP 9 WAVELET DESIGN FOR FIG. 6
aci loss
= 10.^( x_imbal_aci / 10. ) ;
= xebno * errV_aci * x_g_aci ;
                                                                                                                                                                                                                                                                                                                                                                                                                 STEP 9.2 WAVELET TIME RESPONSE "hn"
                                                                                                                                                                                                                     'Sample index Wavelet response' [(0:m)' hn(m+1:2*m+1)']
                                                                                                                            %==== end of iterations
                                                                                                                                                                                                                                                            0.9499
0.98485
0.98685
0.94848
0.94848
0.2428
0.2428
0.0019
0.0019
0.0000
0.0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 1.0000
0.9941
0.9765
0.9476
0.9080
                                                                                                                                                                                                                                                            1.0000
3.0000
5.0000
6.0000
7.0000
9.0000
111.0000
113.0000
115.0000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           1.0000
2.0000
3.0000
4.0000
5.0000
         x_g_aci
xx_aci
%====
                                                                                                                   8====8
                                                                                                                                      end
```

FIG. 51

.800 .734 .662 .586 .586 .343 .343 .263 .114 .114	-0.0135 -0.0666 -0.1117 -0.11485 -0.1766 -0.2073 -0.2065 -0.2065 -0.1795 -0.1795 -0.1795 -0.1335 -0.0769	.018 .035 .035 .035 .035 .035 .113 .113 .112 .107 .038	.041 .024 .007 .009 .025 .038 .050 .060 .067
	17.0000 18.0000 20.0000 21.0000 22.0000 23.0000 24.0000 25.0000 26.0000 27.0000 28.0000 31.0000 32.0000	3.000 6.0000 6.000 6.000 6.000 6.000 6.000 6.000 6.000 6.000 6.0	8.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000

FIG. 5J

.057	.017 .006 .004 .014 .023	. 0 4 5	.037 .037 .031 .018	-0.0029 -0.0095 -0.0155 -0.0208 -0.0287 -0.0311
0.000 1.000 2.000 3.000 5.000	6.000 8.000 9.000 0.000	2.000 2.000 5.000 7.000	8 . 0 . 0 . 0 . 0 . 0 . 0 . 0 . 0 . 0 .	85.0000 86.0000 87.0000 89.0000 91.0000 93.0000

FIG. 5K

```
0.0001
      0.0179
0.0168
0.0154
                         0.0138
                                     0.0103
                                                              0.0036
                                                                           0.0013
0.0187
                                                  0.0067
                                                        0.0051
                                           120.0000
121.0000
122.0000
123.0000
124.0000
                                                                          125.0000
126.0000
127.0000
                        117.0000
113.0000
     114.0000
           115.0000
                                     119.0000
                   116.0000
                                                                                               128.0000
```

38

```
五五
% STEP 10 ITERATION CONVERGENCE IS MEASURED BY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              legend('passband','stopband','deadband','ISI','ACI')
                               CONVERGENCE OF THE LS ERRORS IN
                                                                                                                                                                        plot(err_LS(:,1), err_LS(:,7),'k')
legend('Total LS error relative to iteration=1')
ylabel('Total LS error relative to iteration=1')
                                                                                                                                                                                                                                                                                                                                                                                                                                                           plot(err_LS(:,1), err_LS(:,3), 'k--')
plot(err_LS(:,1), err_LS(:,4), 'k')
plot(err_LS(:,1), err_LS(:,5), 'b')
plot(err_LS(:,1), err_LS(:,6), 'b--')
title('LS ERROR CONTRIBUTORS VS. ITERATION')
                                                                                                                                                                                                                                                   xlabel('Iteration number')
title('TOTAL LS ERROR J VS. ITERATION')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ylabel('LS error relative to total=1')
                                                                                                                                                                                                                                                                                                                                                                                                       plot (err_LS(:,1), err_LS(:,2),'k')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  xlabel('Iteration number')
                                                                figure (1), figure(2)
                                                                                                                                                   figure(1)
                                                                                                                                                                                                                                                                                                                                                                                    figure(2)
                                                                                                                                                                                                                                                                                                                                                                                                                                        hold on
                                                                                                                                                                                                                                                                                                         grid on
                                                                                                                                                                                                                                                                                                                                    hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               grid on
                                                                                                                          % plots
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        hold on
```

FIG. 5L

```
- WAVELET FILTER PERFORMANCE IN figure (3)
- WAVELET RIPPLE, ISI, ACI SNR LOSSES IN figure (4)
                                                                                                                                                                                                                                                                                        x2=length(hw_wsr);
x3=length(hw_wsr);
plot(freq(1:x2)*M,hw_ref, 'b--')
plot(freq(1:x3)*M,hw_wsr, 'b--')
legend('Wavelet response', 'pass & stop templates', 'Wavelet sample
8 STEP 11 PARAMETERS ARE SELECTED TO OPTIMIZE:
                                                                             - WAVELET TIME RESPONSE IN figure (5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     plot (loss LS(:,1), loss LS(:,3), 'k--')
plot (loss_LS(:,1), loss_LS(:,4), 'b')
plot (loss_LS(:,1), loss_LS(:,5), 'b--')
title('SNR_LOSS VS. ITERATION')
legend('total', 'ripple', 'ISI','ACI')
ylabel('SNR_LOSS, dB')
xlabel('Iteration number')
                                                                                                                                                                                                     grid on xlabel('Frequency/Wavelet sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                plot(loss_LS(:,1),loss_LS(:,2),'k')
                                                                                                                                                                                                                                                                                                                                                                                                                              title('WAVELET FREQUENCY RESPONSE')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    xlabel('Time/Wavelet sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ylabel('Wavelet time response')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       title('WAVELET TIME RESPONSE')
                                                                                                                                                                                                                                             ylabel('Power Spectrum, dB')
                                                                                                                                  figure(3)
plot(freq*M, hw_db,'k')
axis([0 200 -100 10])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   axis([0 1.4 -100 0])
hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                axis([-8 8 -0.4 1])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         plot(xx,hn','k')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ', (w:w-)=xx
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              figure (4)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          figure(5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       grid on
hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       xx=xx/M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 grid on
                                                                                                                                                                                                                                                                      hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                      grid on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     hold on
                                                                                                                                                                                                                                                                                                                                                                                                          rate')
```

FIG. 5M

```
8 STEP 12 CALCULATION OF NEW WAVELET WAVEFORM "hn_new"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            STEP 12.2 MATRIX "bw matrix new" FOR MAPPING WAVELET FREQUENCY DESIGN HARMONICS INTO NEWWAVELET IMPULSE RESPONSE IN TIME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             STEP 12.3 MAP WAVELET FREQUENCY DESIGN HARMONICS "hw_eig" INTO NEW WAVELET IMPULSE RESPONSE IN TIME "hn_new"
                                                                                                                                                                                                                   % STEP 12.1 WAVELET SAMPLE INTERVAL "M_new" AND LENGTH "N_new"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Case 2: Fix sampling and dilate M_new = 2^p M hn = hn(n - q M_new) M_new = M*(2^p);
                                                                                                                                                                                                                                                                                                                   Case 1: Fix M_new = M and dilate sampling hn = hn(n 2^{\sim}-p = q M)
                                                                                                                                                                                                                                                                                                                                                                            = n_p for n = n_0 + n_p 2^-p
                                             - "p" SCALE (DILATION)
- "q" TRANSLATION
- "k" FREQUENCY
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                & N is odd
                                                                                                                                                                                                                                                                         8== Wavelet sample interval M_new for:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        N is even
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           N_new = M_new*L+1; % Wavelet length
                     FOR THE PARAMETERS:
                                                                                                                       p=2 % scale change or dilation q=2 % time translation k=3 % frequency translation
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           bw_matrix_new(1,:) = ones(1,n_f);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    nodd= flx( N_new/2 );
nodd = N_new - 2 * nodd ;
if ( nodd == 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            m_{\text{new}} = (N_{\text{new}} - 1) / 2 else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      m_new = N_new/2; %
                                                                                                                                                                                                                                                                                                                                                       n_new = n 2^-p
                                                                                                                                         % Wavelet parameters
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          end
```

FIG. 5N

```
- MOTHER WAVELET "hn"
- NEW WAVELET "hn_new" WITHOUT FREQUENCY TRANSLATION
                                                                                                                                                              hmax 0 = max( abs(hn 0) );

$==== normalized hn 0 is new baseband Wavelet with q=k=0
hn 0 = hn 0/ hmax 0;

$==== hn 1 is hn 0 with translation in time q*M_new
for n=1:N_new+q*M_new
if n <= q*M_new
hn 1(n) = 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                    for n=1:\overline{N} new+q*M new hn_new(n) = hn_1(n)*exp( i*(2*pi*k*(n-1)/(M_new*L)) );
                                                                                                                                                                                                                                                                                                                                                                                       } ==== hn_new is hnl with translation in frequency by k
title('TIME RESPONSE FOR MOTHER, NEW WAVELETS')
                                             STEP 12.4 PLOT WAVELET TIME RESPONSE FOR:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 legend('MOTHER WAVELET','NEW WAVELET')
xlabel('Time/hn\_new sample rate')
ylabel('Wavelet time response')
                                                                                                                                                                                                                                                                                                                hn_1(n) = hn_0(n-q^*M_new);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 xx1 = (L/2)*(1-1/2^p)*M_new;

xx2 = (L/2)*(1+1/2^p)*M_new;

for n=1:N_new+q*M_new

if n<xx1 | n>xx2

hn1(n) = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    x_n = (1:N_new+q*M_new)/M_new;
x_n = x_n-L/2;
plot(x_n,hn1,'k')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                hnl(n) = hn(n-xx1+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             plot (x_n, hn_1, 'k--')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       figure (6)
                                                                                                                                                                                                                                                                                            else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               grid on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    end
                                                                                                                                                                                                                                                                                                                                   end
                                                                                                                                                                                                                                                                                                                                                                        8----
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       end
                                                                                                                                                                                                                                                                                                                                                                                                                                              end
                                                                                                                                                                                                                                                                                                                                                     end
```

FIG. 50

```
arg_rot = twopi* rem( (0:N_new-1)*ich /M_new , 1 );
[freq, hw2_db] = freq_rsp(hn_0, arg_rot, n_fft);
plot(freq*M,hw2_db,'k--')
axis([0 8 -100 10])
% STEP 12.5 PLOT WAVELET FREQUENCY RESPONSE FOR:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               title ('POWER SPECTRUM OF MOTHER, NEW WAVELETS')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  title('POWER SPECTRUM OF MOTHER, NEW WAVELETS')
                                                                                                                                                                                                                      arg_rot = twopi* rem( (0:N-1)*ich /nc , 1 );
[freq, hw_db] = freq_rsp(hn, arg_rot, n_fft);
plot(freq*M, hw_db,'k')
                                                                                 sample rate
                                                                                                             vs. frequency/hn_new sample rate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              %==== plot frequency response of hn, hn_new
                                                                                                                                                                figure(7) % vs. frequency/hn sample rate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              xlabel('Frequency/hn\_new sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          vs. frequency/hn_new sample rate
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        legend ('MOTHER WAVELET', 'NEW WAVELET')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       legend('MOTHER WAVELET','NEW WAVELET')
                                                 - NEW WAVELET "hn_new"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             xlabel('Frequency/hn sample rate')
                         - MOTHER WAVELET "hn"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ylabel('Wavelet time response')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ylabel('Wavelet time response')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  xlabel('Time/hn sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 xlabel('Time/hn sample rate')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  plot(freq*M_new,hw2_db,'k--')
axis([0 8 -100 10])
                                                                                 vs. frequency/hn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ylabel ('Power Spectrum, dB')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ylabel ('Power Spectrum, dB')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                plot(freg*M_new, hw_db,'k')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    figure(8)
                                                                                                                                                                                                  ich = 0;
                                                                                                                                                                                                                                                                                                         hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              hold on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             grid on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  grid on
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           hold on
                                                                                                                                                                                                                                                                                                                                         ich=k;
```

FIG. 5P

```
p_matrix(n+1,ml+1)=1./pi*(an(n+1)*an(ml+1)*(omega_u-omega_l)...
-{ an(ml+1) *ml*( sin( n*omega_u ) - sin( n*omega_l ) ) + ...
an(n+1) *n *( sin(ml*omega_u ) - sin(ml*omega_l ) ) /( ml*n ) + (...
(n+ml)* ( sin( (n-ml)*omega_u ) - sin((n-ml)*omega_l ) ) ...
+(n-ml)*(sin( (n+ml)*omega_u ) -sin((n+ml)*omega_l ) ...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         p_matrix(n+1,m1+1)=1./pi*(an(m1+1)-1.)*(an(n+1)*(omega_u-omega_l)-.....
( sin(n*omega_u )-sin(n*omega_l) ) /n );
end
                                                                                                                                                                                                                                                                                                                                                        p_{\text{matrix}}(n,m): a nXm real, symmetry and positive-definite matrix
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if ( m1 ==n )
if ( n ~= 0)
p_matrix(n+1,ml+1)=1./pi*((an(n+1)*an(n+1)+0.5)*(omega_u-omega_l)-...
2.* an(n+1) * ( sin( n*omega_u )- sin( n*omega_l ) ) ...
/n + (sin(2.* n*omega_u) - sin(2.*n*omega_l))/( 4.* n) );
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              p_matrix(n+1,ml+1)=1./pi*(an(n+1)-1.)*(an(ml+1)*(omega_u-omega_l)-....
( sin(ml*omega_u )-sin( ml*omega_l) ) /ml );
    end
    end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   p_matrix(n+1,m1+1)=1./pi*(an(n+1)-1.)*(an(n+1)-1.)*(omega_u-omega_l);
                                                                                                                                                                                                  compute the real, symmetric, and positive definite matrix input: omega_i: lower edge (radians) omega_u: upper edge (radians)
                                                                                                                                                                                                                                                                                                           an(.): 1xm column vector
                                                                  STEP 13.1 FUNCTION "pmn" COMPUTES MATRIX FOR J(BAND) IN
                                                                                                                                                                                                                                                                                                                                                                                             & STEP 13 FUNCTIONS USED IN MATLAB PROGRAM
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              filter length 'N' 19 odd
                                                                                                                                                                function p_matrix= pmn(omega_l,omega_u, N,an)
                                                                                                                                                                                                                                                                                                                                                                                                                     twopi = 2. * pi;
check filter lenght is odd or even
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      N is even
                                                                                                                                                                                                                                                                                                        N: filter length,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (n == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      1f (m1 == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       end % end of ml loop
end % end of n loop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        nodd = fix(N/2);
nodd = N - 2 * nodd;
if ( nodd == 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                m = (N-1) /2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      e1se
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if ( nodd == 1)
for n= 0:m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for ml= 0:m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      m = N/2;
                                                                                                                                                                                                                                                                                                                                           output
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   end
```

FIG. 50

```
p_matrix(n+1,m1+1) = 1./pi * ( ...
an(n+1) * an(m1+1) * ( omega_u - omega_l ) - ...
an(m1+1)*(sin((n+.5)*omega_u)-sin((n+.5)*omega_l))/( n + 0.5) - ...
an(n+1)*(sin((m1+.5)*omega_u)-sin((m1+.5)*omega_l))/(m1+0.5) + ...
(sin((n-m1)*omega_u) - sin((n-m1)*omega_l))/(2.* (n-m1)) + ...
(sin((n+m1+1)*omega_u)-sin((n+m1+1)*omega_l))/(2.* (n+m1+1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          % STEP 13.2 FUNCTION "freq_rsp" COMPUTES FOURIER TRANSFORM OF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     INPUT "hn" VS. FREQUENCY/WAVELET SAMPLE RATE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             function [freq, hw_db] = freq_rsp(hn, arg_rot, n_freq )
                                                                                                                                                                                      2. * an(n+1) * ( sin( (n+.5) * omega_u) - ...

sin( (n+.5) * omega_l) // (n + 0.5) + ...

( sin( (2*n+1) * omega_u ) -sin( (2*n+1) * omega_l ) ) ...

/( 2. * ( 2.*n + 1) ) ) ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for nf = 1: n_freq
arg=twopi * rem( freq(nf) * ((1:n_filter) -1-m),1);
                                                                                                                                      p_matrix(n+1,m1+1) = 1./pi * ( ... (an(n+1)*an(n+1) + 0.5) * (omega_u - omega_l) - ...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         hw = sum( hn .*exp( (-arg+arg_rot)*i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            in normalized freq interval (0., 0.5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 hw_mag = hw_mag /hw_max;
hw_db = 20.* log10( hw_mag+ 1.e-20);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           & Fourier transform of input hn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          hw_max = max( abs(hw_mag) );
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        end % end of m1 loop
end % end of n loop
l % end of if nodd =1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       hw_mag(nf) = abs(hw);
when N is even
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            % n_freq # of frequency twopi = 2. * pi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         df = 0.5/ (n_freq -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         n_filter = length(hn);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if ( ml == n )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 % frequency response
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       m=(n_filter-1)/2;
freq = (0:df:0.5);
                                                       for m1 = 0:m-1
                         for n = 0:m-1
  end
```

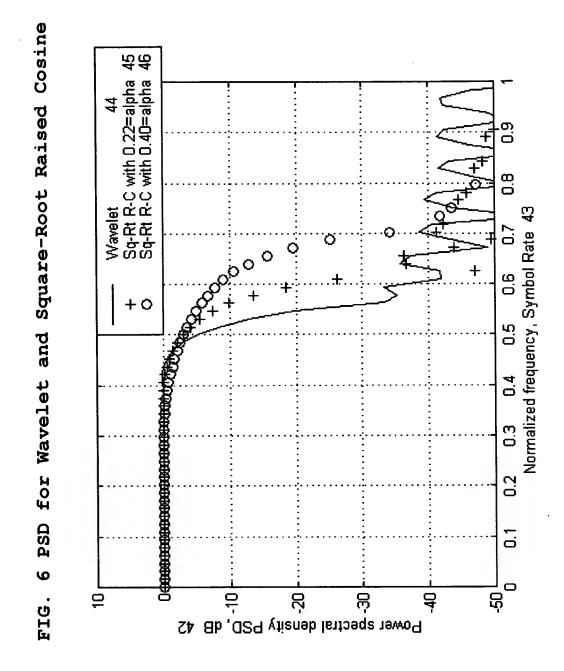
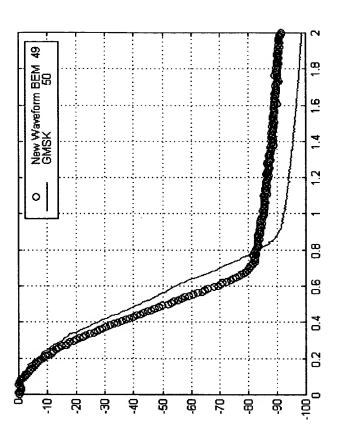


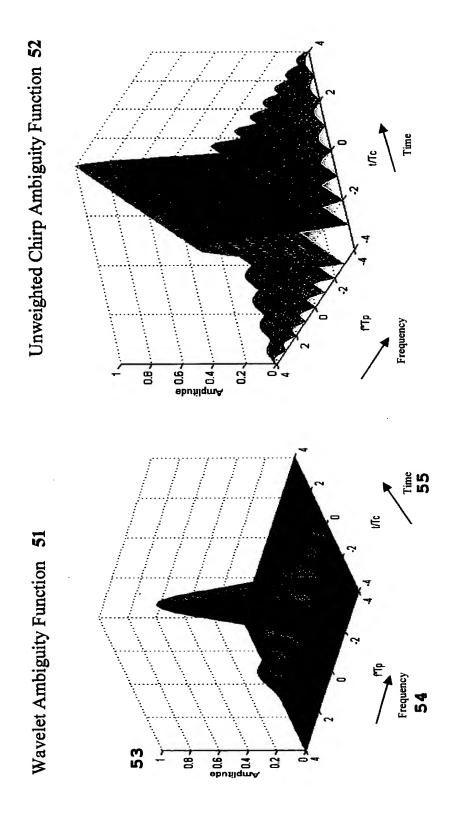
FIG. 7 PSD for New Waveform BEM and GMSK



Normalized frequency, bit rate 48

Power spectral density PSD, dB 47

Radar Ambiguity Functions of Wavelet and Unweighted Chirp Waveform ω FIG.



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